

Unit 4

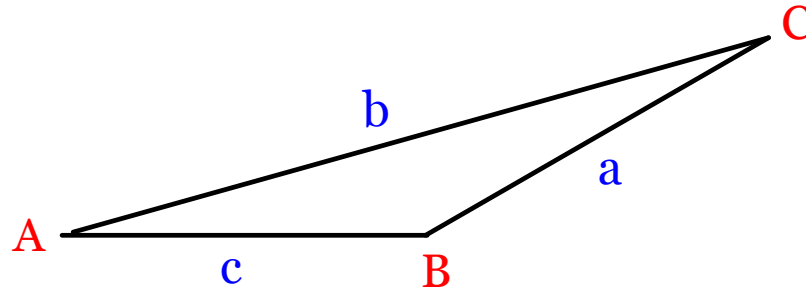
Learning Target 2

I can use the Law of Sines to solve a triangle.

**What is an
oblique
triangle?**

Law of Sines

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$



When to use LAW OF SINES...

AAS - Two angles and a side

ASA - Two angles and the included side

*SSA - Two sides and an angle

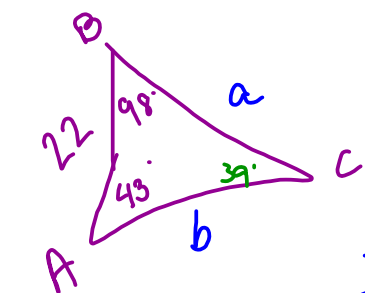
1.) $A = 43^\circ$ $B = 98^\circ$ $c = 22$

$$180^\circ - 43^\circ - 98^\circ = 39^\circ$$

$$\angle C = 39^\circ$$

$$b = 34.62$$

$$a = 23.84$$



$$\frac{a}{\sin 43^\circ} = \frac{b}{\sin 98^\circ} = \frac{22}{\sin 39^\circ}$$

$$\frac{a}{\sin 43^\circ} = \frac{22}{\sin 39^\circ}$$

$$a \sin 39^\circ = 22 \sin 43^\circ$$

$$\frac{a \sin 39^\circ}{\sin 39^\circ} = \frac{22 \sin 43^\circ}{\sin 39^\circ}$$

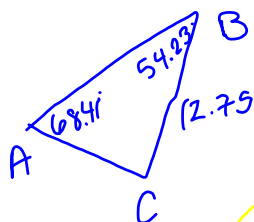
$$a = 23.84$$

$$\frac{b \sin 39^\circ}{\sin 39^\circ} = \frac{22 \sin 98^\circ}{\sin 39^\circ}$$

$$b = 34.62$$

Warm Up 1/5/17

$$A = 68.41^\circ \quad a = 12.75 \quad B = 54.23^\circ$$



$$\angle C = 57.36^\circ$$

$$b = 11.13$$

$$c = 11.55$$

$$\frac{12.75}{\sin 68.41^\circ} = \frac{b}{\sin 54.23^\circ}$$

$$\frac{12.75 \sin 54.23^\circ}{\sin 68.41^\circ} = \frac{b \sin 68.41^\circ}{\sin 68.41^\circ}$$

$$11.13 = b$$

$$\frac{12.75}{\sin 68.41^\circ} = \frac{c}{\sin 57.36^\circ}$$

$$\frac{12.75 \sin 57.36^\circ}{\sin 68.41^\circ} = \frac{c \sin 68.41^\circ}{\sin 68.41^\circ}$$

$$11.55 = c$$

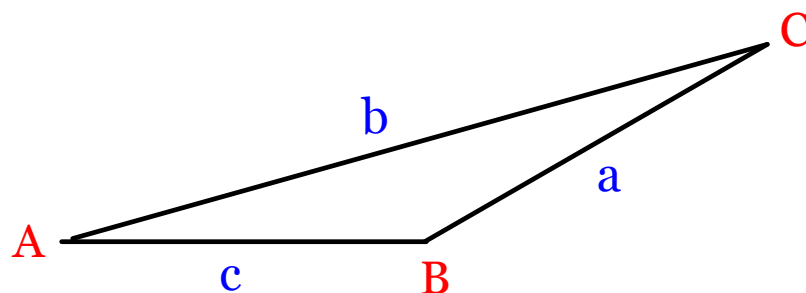
Unit 4

Learning Target 2

I can use the Law of Sines to solve a triangle.

Law of Sines

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$



When to use LAW OF SINES...

AAS - Two angles and a side

ASA - Two angles and the included side

***SSA - Two sides and an angle**

When given SSA there could be . . .

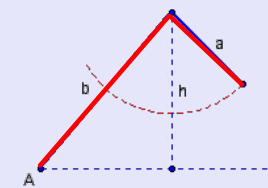
no triangle

one triangle

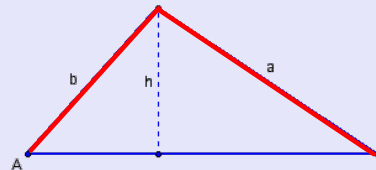
two triangles



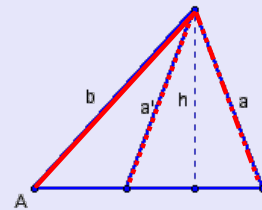
SSA



no triangle possible



One triangle possible



two triangles possible

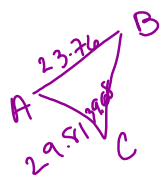
Ambiguous Case



How To Check For More Than One Triangle

- * Solve for the first angle
- * Take that angle and subtract it from 180°
- * Ask yourself, "Can this angle exist with the angle that was given in the original problem?"
(Is their sum more than 180° ?)
- * If the sum is less than 180° , there are two triangles!

3.) $c = 23.76$ $b = 29.81$ $C = 39.68^\circ$



$$\frac{a}{\sin A} = \frac{29.81}{\sin B} = \frac{23.76}{\sin 39.68^\circ}$$

$$\sin^{-1}\left(\frac{29.81 \sin 39.68^\circ}{23.76}\right) = \frac{23.76 \sin B}{23.76}$$

$$53.23^\circ = B$$

$\angle B = 53.23^\circ \xrightarrow{180^\circ - B} \angle B_2 = 126.77^\circ$	$\angle B_2 = 126.77^\circ$
$\xrightarrow{\text{given}} \angle C = 39.68^\circ \xrightarrow{\text{given}} \angle C_2 = 39.68^\circ$	$\angle C_2 = 39.68^\circ$
$\angle A = 87.09^\circ$	$\angle A_2 = 13.55^\circ$
$a = 37.16$	$a_2 = 8.72$

$$\frac{a}{\sin 87.09^\circ} = \frac{23.76}{\sin 39.68^\circ}$$

$$\frac{a \sin 39.68^\circ}{\sin 39.68^\circ} = \frac{23.76 \sin 87.09^\circ}{\sin 39.68^\circ}$$

$$a = 37.16$$

$$\frac{a}{\sin 13.55^\circ} = \frac{23.76}{\sin 39.68^\circ}$$

$$\frac{a \sin 39.68^\circ}{\sin 39.68^\circ} = \frac{23.76 \sin 13.55^\circ}{\sin 39.68^\circ}$$

$$a = 8.72$$