

Introduction

6.4

I can solve trigonometric equations using identities.

IDENTITIES

Quotient Identities

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\cot \theta = \frac{\cos \theta}{\sin \theta}$$

Reciprocal Identities

$$\sin \theta = \frac{1}{\csc \theta}$$

$$\cos \theta = \frac{1}{\sec \theta}$$

$$\tan \theta = \frac{1}{\cot \theta}$$

$$\csc \theta = \frac{1}{\sin \theta}$$

$$\sec \theta = \frac{1}{\cos \theta}$$

$$\cot \theta = \frac{1}{\tan \theta}$$

Pythagorean Identities

$$\star \textcircled{1} \sin^2 \theta + \cos^2 \theta = 1 \quad \star$$

$$\textcircled{2} 1 + \tan^2 \theta = \sec^2 \theta \quad \textcircled{3} 1 + \cot^2 \theta = \csc^2 \theta$$

1b. $\sin^2 \theta = 1 - \cos^2 \theta$

1c. $\cos^2 \theta = 1 - \sin^2 \theta$

2b. $\tan^2 \theta = \sec^2 \theta - 1$

2c. $1 = \sec^2 \theta - \tan^2 \theta$

3b. $\cot^2 \theta = \csc^2 \theta - 1$

3c. $1 = \csc^2 \theta - \cot^2 \theta$

Tips For Using Identities To Simplify Expressions

- * If the expression has multiple trig functions, try to convert all of them to the same trig function.
- * If one or more of the trig functions are squared, try using one of the Pythagorean Identities to rewrite the expression, then simplify to get a factorable expression.
- * When all else fails, turn your expression into sines and cosines.

Simplify the following in terms of SINE.

$$1.) \sin x + \sin x \cot^2 x$$

$$\begin{aligned} & \sin x + \frac{\sin x}{1} \frac{\cos^2 x}{\sin^2 x} \\ & \frac{\sin x \cdot \sin x}{\sin x \cdot 1} + \frac{\cos^2 x}{\sin x} \end{aligned}$$

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$\frac{\sin^2 x}{\sin x} + \frac{\cos^2 x}{\sin x}$

$\frac{\sin^2 x + \cos^2 x}{\sin x}$

$\frac{1}{\sin x}$

Simplify.

4.) $\sin^2 x \cot^2 x + \cos^2 x \tan^2 x$

$$\begin{aligned}
 & \frac{\sin^2 x}{1} \cdot \frac{\cot^2 x}{\sin^2 x} + \cos^2 x \tan^2 x \\
 & \cos^2 x + \cos^2 x \tan^2 x \\
 & \cos^2 x + \frac{\cancel{\cos^2 x} \sin^2 x}{\cancel{\cos^2 x}} \\
 & \cos^2 x + \sin^2 x \\
 & \boxed{1}
 \end{aligned}$$

Simplify.

5.) $2 \cos^2 x - \sin x - 1$