

6.3 Day 2

Solving Trig Equations with Multiple Angles

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Solve each equation over the interval $[0^\circ, 360^\circ]$.

$$1.) \quad 2\sin\theta\cos x + \sqrt{2}\sin\theta = 0$$

$$2\sin\theta\cos x + \sqrt{2}\sin\theta = 0$$

$$\sin\theta(2\cos x + \sqrt{2}) = 0$$

$$\sin\theta = 0$$

$$\theta = 0^\circ, 180^\circ$$

$$2\cos x + \sqrt{2} = 0$$

$$\cos x = -\frac{\sqrt{2}}{2}$$

$$\cancel{3x} = 0^\circ, 180^\circ$$

$$= 360^\circ, 540^\circ$$

$$= 720^\circ, 900^\circ$$

$$x = 135^\circ, 225^\circ$$

$$x = 0^\circ, 60^\circ, 120^\circ, 180^\circ, 240^\circ, 300^\circ, 135^\circ, 225^\circ$$

Solve each equation over the interval $[0, 2\pi)$.

$$2.) \quad 2\cos 2x \tan x = \sqrt{3} \tan x$$

$$-\sqrt{3} \tan x$$

$$2\cos\theta \tan x - \sqrt{3} \tan x = 0$$

$$\tan x(2\cos\theta - \sqrt{3}) = 0$$

$$\tan x = 0 \quad 2\cos\theta - \sqrt{3} = 0$$

$$x = 0, \pi, \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}$$

$$\frac{2\cos\theta - \sqrt{3}}{2} = 0$$

$$\cos\theta = \frac{\sqrt{3}}{2}$$

$$\theta = \frac{\pi}{6}, \frac{11\pi}{6}$$

$$\frac{11\pi}{6}$$

$$\frac{1}{2}x = \frac{\pi}{6} \cdot \frac{1}{2}, \frac{11\pi}{6} \cdot \frac{1}{2}$$

$$= \frac{13\pi}{12}, \frac{23\pi}{12}$$

$$\left\{ \begin{array}{l} \frac{\pi}{6} + \frac{2\pi \cdot 6}{12} \\ \frac{\pi}{6} + \frac{12\pi}{6} \end{array} \right.$$