

ebra

ctice

Name: KEY

Date: _____ Period: _____

Solve each equation over the interval $[0, 2\pi)$. If necessary, round answers to the nearest hundredths.

1.) $6\sin^2 x - 3 = 2\sin^2 x$

$$\begin{aligned} 4\sin^2 x &= 3 \\ \sqrt{\sin^2 x} &= \sqrt{\frac{3}{4}} \\ \sin x &= \pm \frac{\sqrt{3}}{2} \end{aligned}$$

$$x = \frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3}$$

3.) $\cot x - 2 = 0$

$$\begin{aligned} \cot x &= 2 \\ \tan x &= \frac{1}{2} \\ x' &= .46 \end{aligned}$$

$$x = -.46, 3.61$$

5.) $5\tan x = 3\tan x$

$$2\tan x = 0$$

$$\tan x = 0$$

$$x = 0, \pi$$

2.) $3\cos x - 5 = 7\cos x - 4$

$$\begin{aligned} -1 &= 4\cos x \\ \cos x &= -\frac{1}{4} \\ x' &= 1.32 \end{aligned}$$

$$x = 1.82, 4.46$$

4.) $5\csc^2 x - 1 = 4$

$$\begin{aligned} 5\csc^2 x &= 5 \\ \sqrt{\csc^2 x} &= \sqrt{1} \\ \csc x &= \pm 1 \end{aligned}$$

$$x = \frac{\pi}{2}, \frac{3\pi}{2}$$

6.) $-3\sec^2 x + 4 = -2$

$$\begin{aligned} -3\sec^2 x &= -6 \\ \sqrt{\sec^2 x} &= \sqrt{2} \\ \sec x &= \pm \sqrt{2} \end{aligned}$$

$$x = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$$

Solve each equation over the interval $[0^\circ, 360^\circ]$. If necessary, round answers to the nearest hundredths.

7.) $\tan^2 x - 3 = 0$

$$\sqrt{\tan^2 x} = \sqrt{3}$$

$$\tan x = \pm \sqrt{3}$$

$$x = 60^\circ, 120^\circ, 240^\circ, 300^\circ$$

8.) $20 \sin x + 1 = 3$

$$20 \sin x = 2$$

$$\sin x = \frac{1}{10}$$

$$x' = 5.74^\circ$$

~~S | A~~
T C

$$x = 5.74^\circ, 174.26^\circ$$

9.) $\cos x - 7 = 0$

$$\cos x = 7$$

No Solution

10.) $8 \tan x + 13 = 3 \tan x + 2$

$$5 \tan x = -11$$

$$\tan x = -\frac{11}{5}$$

$$x' = 65.56^\circ$$

~~S | A~~
T O

$$x = 114.44^\circ \\ \text{and} \\ 294.44^\circ$$

11.) $\sin x - 3 = 5 \sin x$

$$-3 = 4 \sin x$$

$$\sin x = -\frac{3}{4}$$

$$x' = 48.59^\circ$$

~~S | A~~
T O

$$x = 228.59^\circ$$

$$\text{and} \\ 311.41^\circ$$

12.) $3 \sec^2 x - 4 = 0$

$$\sqrt{3 \sec^2 x} = \sqrt{\frac{4}{3}}$$

$$\sec x = \pm \frac{2}{\sqrt{3}}$$

$$\cos x = \pm \frac{\sqrt{3}}{2}$$

$$x = 30^\circ, 150^\circ, 210^\circ, 330^\circ$$