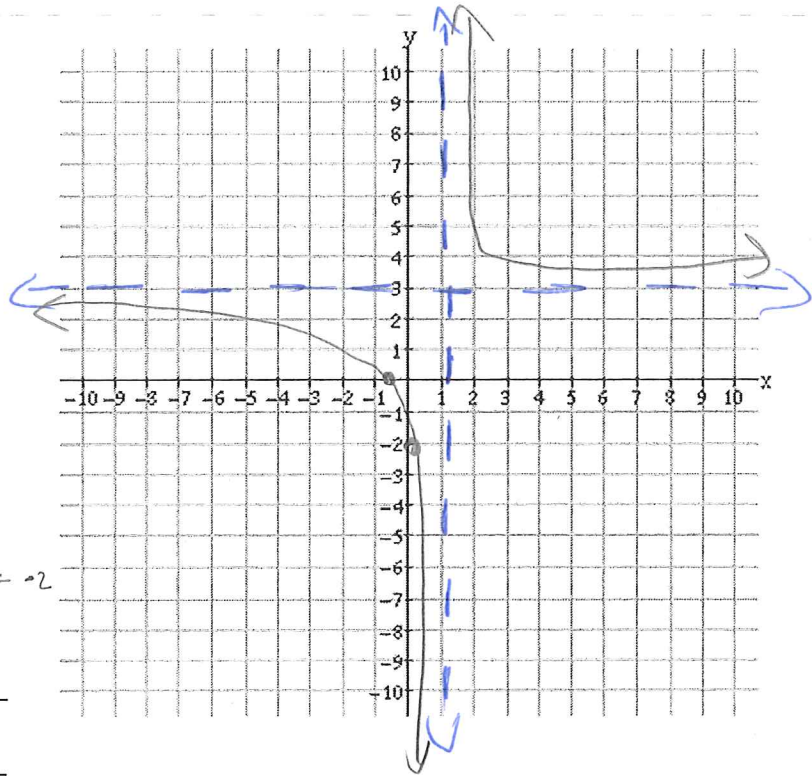


Identify the key information for the following rational functions, then graph.

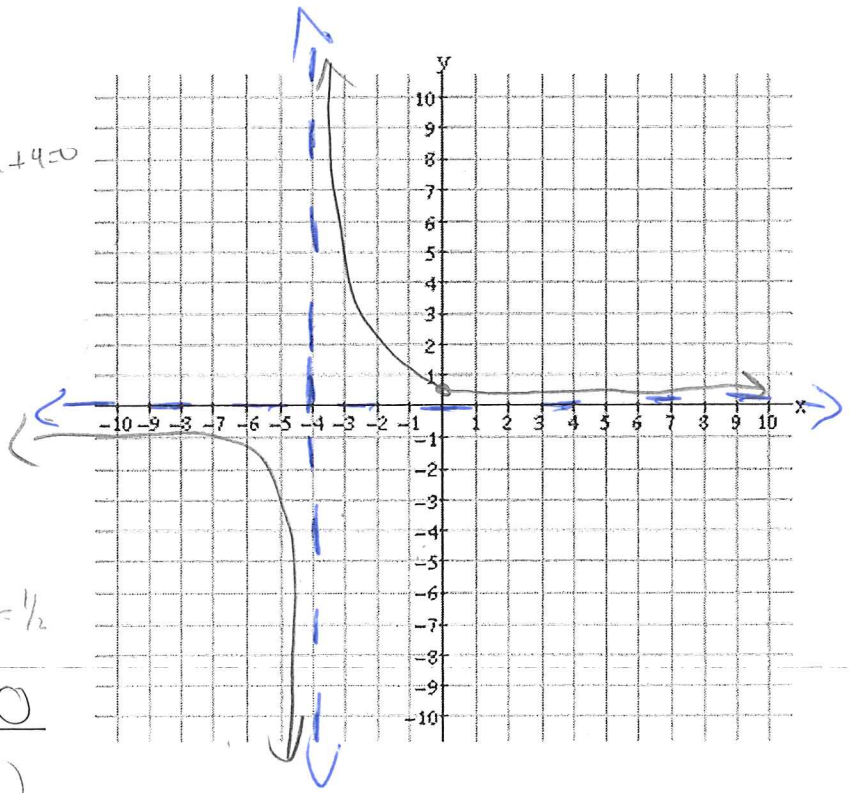
1.) $f(x) = \frac{3x+2}{x-1}$

- a. Vertical Asymptote(s): $x=1$ $x-1=0$
- b. Horizontal Asymptote: $y=3$ $y=\frac{3}{1}$
- c. Hole(s): none
- d. Domain: $(-\infty, 1) \cup (1, \infty)$
- e. Range: $(-\infty, 3) \cup (3, \infty)$
- f. ^{zeros} x-intercept(s): $(-\frac{2}{3}, 0)$ $3x+2=0$
 $x=-\frac{2}{3}$
- g. y-intercept: $(0, -2)$ $\frac{3(0)+2}{0-1} = \frac{2}{-1} = -2$
- h. End behavior: As $x \rightarrow -\infty, f(x) \rightarrow$ 3
As $x \rightarrow \infty, f(x) \rightarrow$ 3



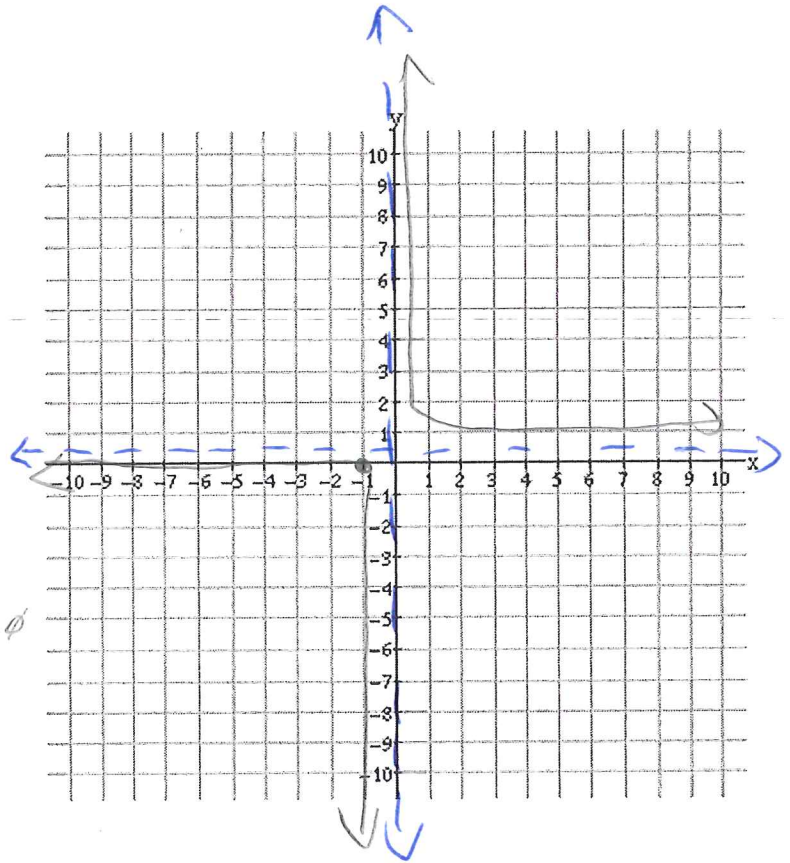
2.) $f(x) = \frac{2}{x+4}$

- a. Vertical Asymptote(s): $x=-4$ $x+4=0$
- b. Horizontal Asymptote: $y=0$
- c. Hole(s): none
- d. Domain: $(-\infty, -4) \cup (-4, \infty)$
- e. Range: $(-\infty, 0) \cup (0, \infty)$
- f. ^{zeros} x-intercept(s): none $2 \neq 0$
- g. y-intercept: $(0, \frac{1}{2})$ $\frac{2}{0+4} = \frac{2}{4} = \frac{1}{2}$
- h. End behavior: As $x \rightarrow -\infty, f(x) \rightarrow$ 0
As $x \rightarrow \infty, f(x) \rightarrow$ 0



3.) $f(x) = \frac{x+1}{2x}$

- a. Vertical Asymptote(s): $x=0$ $2x=0$
- b. Horizontal Asymptote: $y = \frac{1}{2}$ $y = \frac{1}{2}$
- c. Hole(s): none
- d. Domain: $(-\infty, 0) \cup (0, \infty)$
- e. Range: $(-\infty, \frac{1}{2}) \cup (\frac{1}{2}, \infty)$
- f. x-intercept(s): $(-1, 0)$ $x+1=0$
- g. y-intercept: none $\frac{0+1}{2(0)} = \frac{1}{0} = \emptyset$
- h. End behavior: As $x \rightarrow -\infty, f(x) \rightarrow \frac{1}{2}$
 As $x \rightarrow \infty, f(x) \rightarrow \frac{1}{2}$



4.) $f(x) = \frac{-8}{x(x+3)}$

- a. Vertical Asymptote(s): $x=0$ $x=-3$ $\begin{cases} x=0 \\ x+3=0 \end{cases}$
- b. Horizontal Asymptote: $y=0$
- c. Hole(s): none
- d. Domain: $(-\infty, -3) \cup (-3, 0) \cup (0, \infty)$
- e. Range: $(-\infty, 0) \cup (0, \infty)$
- f. x-intercept(s): none $0 = -8$
- g. y-intercept: none $\frac{-8}{0(0+3)} = \frac{-8}{0} = \emptyset$
- h. End behavior: As $x \rightarrow -\infty, f(x) \rightarrow 0$
 As $x \rightarrow \infty, f(x) \rightarrow 0$

