

Write a function in standard form of minimum degree with given zeros and multiplicities.

1.) 6 multiplicity of 2; 1 multiplicity of 1

$$(x-6)(x-6)(x-1)$$

$$(x^2 - 12x + 36)(x-1)$$

$$\begin{array}{r} x^3 - 12x^2 + 36x \\ - x^2 + 12x - 36 \\ \hline \end{array}$$

$$f(x) = x^3 - 13x^2 + 48x - 36$$

2.) -1; 1; and 0 multiplicity of 2

$$(x+1)(x-1)(x)(x)$$

$$(x^2 - 1)(x^2)$$

$$f(x) = x^4 - x^2$$

3.) 1; 1; 2

$$(x-1)(x-1)(x-2)$$

$$(x^2 - 2x + 1)(x-2)$$

$$\begin{array}{r} x^3 - 2x^2 + x \\ - 2x^2 + 4x - 2 \\ \hline \end{array}$$

$$f(x) = x^3 - 4x^2 + 5x - 2$$

4.) 4 multiplicity of 1; -3 multiplicity of 2

$$(x-4)(x+3)(x+3)$$

$$(x-4)(x^2 + 6x + 9)$$

$$\begin{array}{r} x^3 + 6x^2 + 9x \\ - 4x^2 - 24x - 36 \\ \hline \end{array}$$

$$f(x) = x^3 + 2x^2 - 15x - 36$$

5.) 2; and 5 with a multiplicity of 2

$$(x-2)(x-5)(x-5)$$

$$(x-2)(x^2 - 10x + 25)$$

$$\begin{array}{r} x^3 - 10x^2 + 25x \\ - 2x^2 + 20x - 50 \\ \hline \end{array}$$

$$f(x) = x^3 - 12x^2 + 45x - 50$$

6.)  $\frac{1}{2}$ ; 2; -3

$$(x-2)(x+3)(2x-1)$$

$$(x^2 + x - 6)(2x-1)$$

$$\begin{array}{r} 2x^3 + 2x^2 - 12x \\ - x^2 - x + 6 \\ \hline \end{array}$$

$$f(x) = 2x^3 + x^2 - 13x + 6$$

Write an equation in vertex form for the quadratic function given the vertex and a point on the graph.

79.) vertex  $(-3, 0)$ , passing through  $(-5, -4)$

$$-4 = A(-5+3)^2 + 0$$

$$-4 = 4A$$

$$-1 = A$$

$$f(x) = -1(x+3)^2$$

810.) vertex  $(0, 1)$ , passing through  $(-1, 0)$

$$0 = A(-1-0)^2 + 1$$

$$0 = A(-1)^2 + 1$$

$$-1 = 1A$$

$$-1 = A$$

$$f(x) = -1(x)^2 + 1$$

911.) vertex  $(2, 5)$ , passing through  $(3, 7)$

$$7 = A(3-2)^2 + 5$$

$$7 = 1A + 5$$

$$2 = A$$

$$f(x) = 2(x-2)^2 + 5$$

1012.) vertex  $(-3, 4)$ , passing through  $(0, 0)$

$$0 = A(0+3)^2 + 4$$

$$0 = 9A + 4$$

$$-4 = 9A$$

$$-4/9 = A$$

$$f(x) = -4/9(x+3)^2 + 4$$

Write an equation for a linear function given the following:

113.)  $f(-4) = -2$  and  $f(-3) = 5$   
 $(-4, -2)$   $(-3, 5)$

$$\frac{5 - (-2)}{-3 - (-4)} = \frac{7}{1} = 7$$

$$y + 2 = 7(x + 4)$$

$$y + 2 = 7x + 28$$

$$y = 7x + 26$$

$$f(x) = 7x + 26$$

114.)  $f(4) = -2$  and  $f(-4) = -4$   
 $(4, -2)$   $(-4, -4)$

$$\frac{-4 - (-2)}{-4 - 4} = \frac{-2}{-8} = \frac{1}{4}$$

$$y + 2 = 1/4(x - 4)$$

$$y + 2 = 1/4x - 1$$

$$y = 1/4x - 3$$

$$f(x) = 1/4x - 3$$

115.)  $f(-4) = 2$  and  $f(0) = -5$

$(-4, 2)$   $(0, -5)$

$$\frac{-5 - 2}{0 - (-4)} = \frac{-7}{4}$$

$$f(x) = -7/4x - 5$$

116.)  $f(0) = -2$  and  $f(-5) = 3$

$(0, -2)$   $(-5, 3)$

$$\frac{3 - (-2)}{-5 - 0} = \frac{5}{-5} = -1$$

$$f(x) = -x - 2$$