

Verify the following identities.

1.)  $(\sin^2 \theta + \cos^2 \theta)^3 = 1$

$$(1)^3 = 1$$

$$1 = 1$$



2.)  $(\sin x + \cos x)^2 = 1 + 2\sin x \cos x$

$$(\sin x + \cos x)(\sin x + \cos x)$$

$$\sin^2 x + 2\sin x \cos x + \cos^2 x$$

$$1 + 2\sin x \cos x$$

$$= 1 + 2\sin x \cos x$$



3.)  $\frac{\sec^2 x - 1}{\sec^2 x} = \sin^2 x$

$$\frac{\tan^2 x}{\sec^2 x} = \sin^2 x$$

$$\tan^2 x \cdot \frac{1}{\sec^2 x} = \sin^2 x$$

$$\frac{\sin^2 x}{\cancel{\cos^2 x}} \cdot \frac{\cancel{\cos^2 x}}{1} = \sin^2 x$$

$$\sin^2 x = \sin^2 x$$



4.)  $\tan^4 x = \tan^2 x \sec^2 x - \tan^2 x$

$$\tan^4 x = \tan^2 x (\sec^2 x - 1)$$

$$\tan^4 x = \tan^2 x (\tan^2 x)$$

$$\tan^4 x = \tan^4 x$$



Verify the following identities.

5.)  $\tan^2 x + 5 = \sec^2 x + 4$

$$(\sec^2 x - 1) + 5 = \sec^2 x + 4$$

$$\sec^2 x - 1 + 5 = \sec^2 x + 4$$

$$\sec^2 x + 4 = \sec^2 x + 4$$



6.)  $\frac{\tan x \cot x}{\cos x} = \sec x$

$$\tan x \cdot \cot x \cdot \frac{1}{\cos x} = \sec x$$

$$\frac{\cancel{\sin x}}{\cancel{\cos x}} \cdot \frac{\cancel{\cos x}}{\cancel{\sin x}} \cdot \frac{1}{\cos x} = \sec x$$

$$\frac{1}{\cos x} = \sec x$$

$$\sec x = \sec x$$



7.)  $\csc^4 x - \cot^4 x = 2 \csc^2 x - 1$

$$(\csc^2 x - \cot^2 x)(\csc^2 x + \cot^2 x)$$

$$(1)(\csc^2 x + \cot^2 x)$$

$$\csc^2 x + \cot^2 x = 2 \csc^2 x - 1$$

$$\csc^2 x + (\csc^2 x - 1) = 2 \csc^2 x - 1$$

$$2 \csc^2 x - 1 = 2 \csc^2 x - 1$$



8.)  $\cos x \sec x - \cos^2 x = \sin^2 x$

$$\frac{\cancel{\cos x}}{1} \cdot \frac{1}{\cancel{\cos x}} - \cos^2 x = \sin^2 x$$

$$1 - \cos^2 x = \sin^2 x$$

$$\sin^2 x = \sin^2 x$$

