

Chapter 7

I can verify Identities with multiplying

REMEMBER...

- * **Work with the more "complicated" side**
- * **Use the other side to help you decide what to substitute in the "complicated" side**
- * **Use Reciprocal, Quotient, Pythagorean Identities**
- * **If stuck, change everything to sines & cosines**

$$1.) (1 - \sin \theta)(1 + \sin \theta) = \cos^2 \theta$$

$$1 + \cancel{\sin \theta} - \cancel{\sin \theta} - \sin^2 \theta = \cos^2 \theta$$

$$1 - \sin^2 \theta = \cos^2 \theta$$

$$\cos^2 \theta = \cos^2 \theta \quad \checkmark$$

$$2.) \csc x (\cos x + \sin x) = \cot x + 1$$

$$\csc x \cos x + \csc x \sin x = \cot x + 1$$

$$\frac{1}{\sin x} \frac{\cos x}{1} + \frac{1}{\cancel{\sin x}} \frac{\cancel{\sin x}}{1} = \cot x + 1$$

$$\frac{\cos x}{\sin x} + 1 = \cot x + 1$$

$$\cot x + 1 = \cot x + 1 \quad \checkmark$$

$$\begin{aligned}
 3.) \quad & \sin^2 x (\sec^2 x + \csc^2 x) = \sec^2 x \\
 & \sin^2 x \sec^2 x + \sin^2 x \csc^2 x = \sec^2 x \\
 & \frac{\sin^2 x}{\cos^2 x} + \sin^2 x \csc^2 x = \sec^2 x \\
 & \underbrace{\frac{\sin^2 x}{\cos^2 x}}_{\tan^2 x} + \cancel{\sin^2 x} \frac{1}{\cancel{\sin^2 x}} = \sec^2 x \\
 & \tan^2 x + 1 = \sec^2 x \\
 & \sec^2 x = \sec^2 x \quad \checkmark
 \end{aligned}$$

$$x^2 = x \cdot x \quad 5^2 = 5 \cdot 5$$

$$\begin{aligned}
 4.) \quad & (\sin x + \cos x)^2 = 1 + 2 \sin x \cos x \\
 & (\sin x + \cos x)(\sin x + \cos x) = 1 + 2 \sin x \cos x \\
 & \sin^2 x + \underbrace{\sin x \cos x} + \underbrace{\cos x \sin x} + \cos^2 x \\
 & \sin^2 x + 2 \sin x \cos x + \cos^2 x \\
 & \hline
 & 1 + 2 \sin x \cos x = 1 + 2 \sin x \cos x \quad \checkmark
 \end{aligned}$$