

* Answers may vary *

Verify each of the following identities.

1. $\frac{1}{\sec^2 x} + \frac{1}{\csc^2 x} = 1$

$$\cos^2 x + \sin^2 x =$$

$$1 = 1$$

2. $\sec^2 x - \tan^2 x + \cot^2 x = \csc^2 x$

$$1 + \cot^2 x =$$

$$\csc^2 x = \csc^2 x$$

3. $\cos^2 x(1 + \tan^2 x) = 1$

$$\cos^2 x (\sec^2 x) =$$

$$\cos^2 x \left(\frac{1}{\cos^2 x} \right)$$

$$1 = 1$$

4. $2\cos^2 x - 1 = 1 - 2\sin^2 x$

$$2(1 - \sin^2 x) - 1 =$$

$$2 - 2\sin^2 x - 1 =$$

$$1 - 2\sin^2 x = 1 - 2\sin^2 x$$

5. $\csc^2 x \tan^2 x - 1 = \tan^2 x$

$$\frac{1}{\cancel{\sin^2 x}} \cdot \frac{\sin^2 x}{\cos^2 x} - 1 =$$

$$\frac{1}{\cos^2 x} - 1 =$$

$$\sec^2 x - 1 =$$

$$\tan^2 x = \tan^2 x$$

6. $\frac{\cot x}{\csc x} = \cos x$

$$\frac{\frac{\cos x}{\sin x}}{1/\sin x}$$

$$\frac{\cos x}{\sin x} \cdot \frac{\sin x}{1}$$

$$\cos x = \cos x$$

7. $\cos^2 x - \sin^2 x = 1 - 2\sin^2 x$

$$1 - \sin^2 x - \sin^2 x =$$

$$1 - 2\sin^2 x = 1 - 2\sin^2 x$$

8. $\frac{1 + \cot^2 x}{\csc x} = \csc x$

$$\frac{\csc^2 x}{\csc x} =$$

$$\csc x = \csc x$$